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| **Year 11 Specialist Mathematics**  Semester 2, October 2020  **Test 6: Complex Numbers and Number Proofs**  **Calculator Free Weighting: 6%**  **[Australian Curriculum Reference Numbers: 2.3.1 - 2.3.16]** |

**Total Time: 50min Total Marks =**

**Student Name:**

**Teacher: \_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_**

**INSTRUCTIONS TO STUDENTS:**

* You **are not allowed** a calculator or any notes.
* A formula booklet will be provided.

You are required to attempt ALL questions.

Write answers in the spaces provided beneath each question.

Marks are shown with the questions.

**Show all working** clearly, in sufficient detail to allow your answers to be checked readily and for marks to be answered for reasoning. Incorrect answers given without supporting reasoning cannot be allocated any marks. For any question or part question worth more than two marks, valid working or justification is required to receive full marks.

1. Given that and , determine the following:   
    (express your answers in the form , where and are real)

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[1,2,1,3 = 7 marks]

1. Prove that any complex number multiplied by its conjugate will always give a real number.

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[3 marks]

1. Prove that , for every positive integer .

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**[8 Marks]**

1. For the equation
   1. ***Show*** that is a complex solution.

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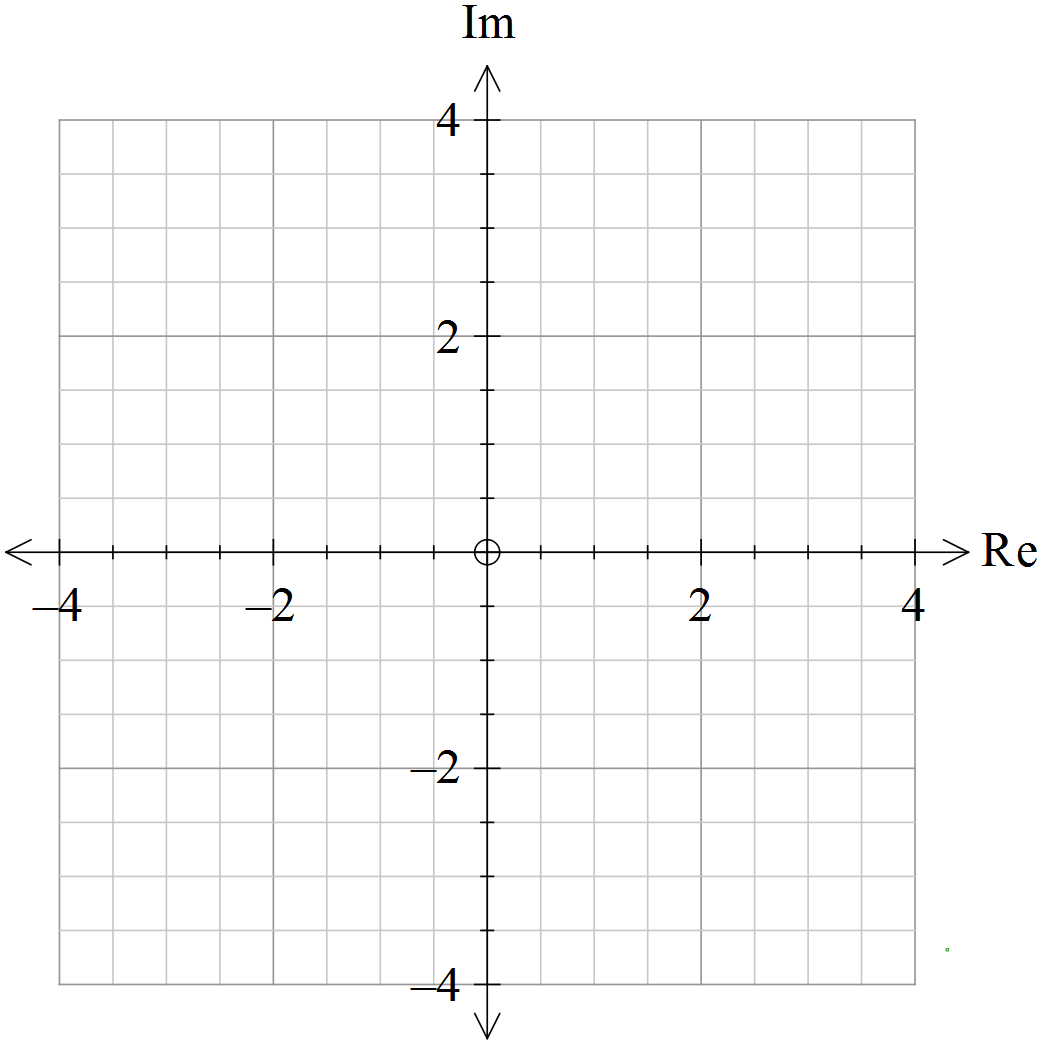
* 1. Determine the other two solutions to the equation and hence factorise .

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**[5,3 = 8 Marks]**

1. Sketch the complex numbers as vectors on the Argand Diagram below.

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[5 marks]

1. Complete the square to express as a product of linear factors.

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[3 marks]

1. For the Argand Diagrams below:

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| * 1. Sketch | * 1. Sketch |
| * 1. Sketch | * 1. Sketch |

[4 marks]

1. Convert the decimal into the form where are coprime.

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[4 marks]

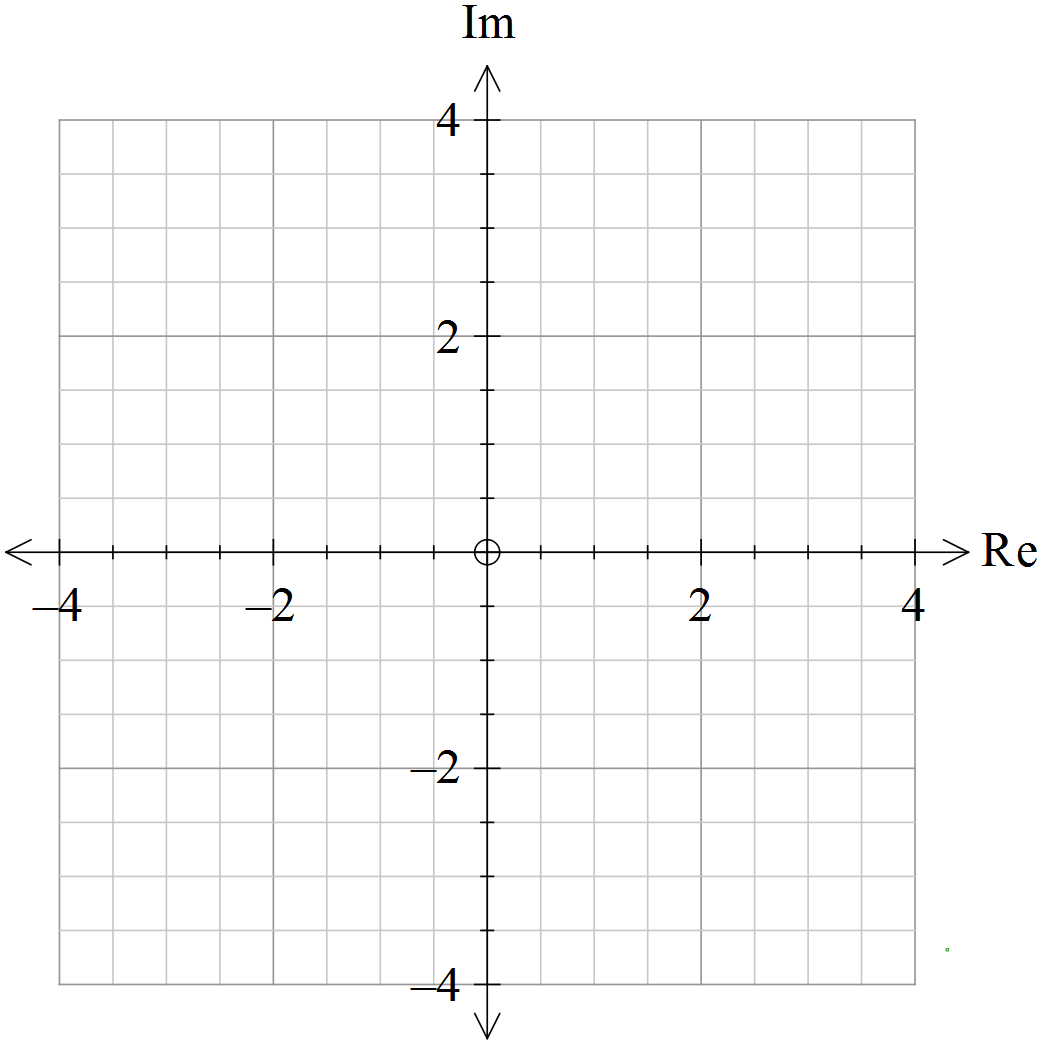
1. Use proof by exhaustion to prove that there are no rational solutions to the equation:

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**[8 Marks]**

\*\*\* End of Test \*\*\*

\*\*\*Extra space for working out\*\*\*



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